Introduction

## Welcome in the Netherlands and in Delft



#### Introduction

### Welcome to our Finite Element Course!

#### Domenico Lahaye



#### Mathias Müller



Introduction

# Why Finite Elements? FE = An Old Guy in Good Shape!



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Introduction

### What is Finite Elements?



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Introduction

### What is our Course About?

- algorithmic aspects
- simple model problems
- spatial and temporal variation

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Introduction

#### What is this Course Not?

#### mathematical foundations

advanced engineering applications

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- build your own finite element code
- for elliptic and parabolic differential equations
- acquire know-how to extend the code to more complex cases

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# How is this course organized (1/4): Lectures

- Day 1: Motivation, Model problems and Tools
- Day 2: Theory and Algorithms for Spatial Discretization
- Day 3: Theory and Algorithms for Time Discretization
- Day 4: Convection/Diffusion Two Dimensinal Problem
- Day 5: The Quest for Accurary Extensions

# How is this course organized (2/4): Lab Sessions

- Day 1: Introduction to Matlab (or Python)
- Day 2: Implementation of Spatial Discretization in Matlab/Python

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- Day 3: Implementation of Temporal Discretization
- Day 4: Extension to 2D
- Day 5: Convection/Diffusion

# How is this course organized (3/4): Location

- Location of the lectures: daily 10:00 13:00
  - Tuesday: Drebbelweg Zaal 2
  - Wednesday: EWI Lecture Hall Ampere
  - Thursday: EWI Lecture Hall L (tricky to find)

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• Friday: IO Joost van Grinten

## How is this course organized (4/4): Location

- Location of the lab sessions: daily 10:00 13:00
  - Monday, Tuesday, Wednesday: TBM Computer Room B

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• Thursday, Friday: LR Computer Room 007

Introduction

#### **Course Assesment**

- no exam as such
- active participation during the lectures
- completion of the programming exercises

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• increase  $\delta$ !

Introduction



An Example from Computational Electromagnetics



- Introduction
- An Example from Computational Electromagnetics

• Humble beginnings

An Example from Computational Electromagnetics

# Motivating Example Inductive Fault Current Limiter



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# Motivating Example Current through AC winding - Line current



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# Motivating Example Magnetic Flux Contributions





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# Motivating Example Total Magnetic Flux and Field

#### Magnetic Flux



#### Magnetic Field



An Example from Computational Electromagnetics

## **Motivating Example**

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### **Mathematical Model**

• 
$$\sigma \frac{\partial u}{\partial t} + \nabla(\mu \nabla u) = f$$

*u*: magnetic potential *f*: current

 $\sigma$  and  $\mu$ : material parameters

• 
$$\nabla(\mu \nabla u) = f$$
 ( $\sigma = 0$ )

An Example from Computational Electromagnetics

# Motivating Example Three Reoccuring Themes

• theme 1: discontinuous coefficients

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- theme 2: singular domains
- theme 3: time evolution

Humble beginnings



- Introduction
- An Example from Computational Electromagnetics

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• Humble beginnings

Humble beginnings

## **Humble Beginnings**

#### Study Goals

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- classify partial differential equations
- apply integration theorems
- (Become acquanted with variational calculus)